BMVC 2016 Tutorial: Measurement Based Appearance Modelling



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Material reflectance capture techniques



BRDF



SVBRDF





Surface appearance

- Bidirectional Reflectance Distribution Function (BRDF)
 - 4D general case, 3D isotropic
 - Surface reflection at one surface point
- Spatially Varying BRDF (SVBRDF)
 - 6D, BRDF per surface point
- Bidirectional Texture Function (BTF)
 - 6D, more general includes inter-reflection & scattering
 - Data-driven representation of reflectance functions







BRDF



• Defined as the ratio of reflected radiance to incident irradiance:

$$f_r(\mathbf{x}, \omega_r, \omega_i) = dL_r(\mathbf{x}, \omega_r)/dE_i(\mathbf{x}, \omega_i)$$
$$= dL_r(\mathbf{x}, \omega_r)/(L_i(\mathbf{x}, \omega_i) \cos\theta \, d\omega_i)$$

- the units of a BRDF are inverse steradian [1/sr].

BRDF



• Physically based BRDFs have 2 important properties: Helmholtz Reciprocity: $f_r(x, \omega_r, \omega_j) = f_r(x, \omega_j, \omega_r)$. and

Energy Conservation: $\int_{\Omega} f_r(\mathbf{x}, \omega_r, \omega_i) \cos\theta_i d\omega_i \leq 1$, for all ω_r in Ω .

Reflection Models

- Mathematical representation a class of BRDFs
 - typically with a small number of parameters
- Types of BRDF models
 - Phenomenological
 - Physically based
- Parameter fitting
 - Measured data

Phenomenological Models

- Equations that describe the "qualitative behavior" of surfaces
 - matte, glossy or plastic, roughness
- Examples
 - Lambertian diffuse reflection
 - Phong specular reflection [Phong75]

Lambertian Reflection



- $f_r(\omega_r, \omega_i) = \rho_d / \pi$
 - $-\rho_d$ is the diffuse reflection coefficient [0,1]
 - $\pi = \int_{\Omega} \cos\theta \, d\omega$, is the normalization constant!
 - Well suited for measurements

Glossy and Retro-reflective



- Glossy surfaces plastic, high gloss paints, polished wood
- Retro-reflective velvet, moon's surface, road signs, bike reflectors

Blinn-Phong Model

 $\omega_{\rm h} = (\omega_{\rm i} + \omega_{\rm o})/||\omega_{\rm i} + \omega_{\rm o}||$



•
$$f_r(\omega_o, \omega_i) = \rho_d / \pi + \rho_s (n \cdot \omega_h)^s / (n \cdot \omega_i)$$

= $\rho_d / \pi + \rho_s (\cos\theta)^s / (n \cdot \omega_i)$



Lafortune Generalized Cosine Lobe





Fits to measured data

- $f_r(\omega_{r,}\omega_{i}) = \rho_d/\pi + \sum_j [C_{x,j}(\omega_{i,x}\cdot\omega_{r,x}) + C_{y,j}(\omega_{i,y}\cdot\omega_{r,y}) + C_{z,j}(\omega_{i,z}\cdot\omega_{r,y})]^{s,j}$
 - Off-specularity, retro-reflection, anisotropy
 - Well suited for measured data!

Ward Anisotropic Model

Generlization of microfacet model to account for anisotropy!



- $f_r(\omega_r, \omega_i) = \rho_d / \pi + \rho_s$ 1 $exp[-tan^2\delta(cos^2\phi/\alpha_x^2 + sin^2\phi/\alpha_y^2)]$ $\sqrt{cos\theta_i cos\theta_r}$ $4\pi\alpha_x\alpha_y$
 - elliptical Gaussians, $\alpha_x \& \alpha_y$ control standard deviation in x & y
 - energy preserving & reciprocal

Physically Based: Microfacet Model



- $f_r(\omega_r, \omega_j) = \frac{D(\omega_h) G(\omega_r, \omega_j) F_r(\omega_h)}{4 (n \cdot \omega_j) (n \cdot \omega_r)}$
 - D, the distribution term
 - G, the geometric term
 - F, the Fresnel term

Torrance-Sparrow Model

- $D(\omega_h) = \exp[\tan \delta/m]^2$ Beckman distribution $m^2 \cos^4 \delta$
 - $-\delta$, angle between n and ω_h
 - m, root-mean-square slope of microfacets

•
$$G(\omega_r, \omega_i) = \min\{1, 2 (n \cdot \omega_h) (n \cdot \omega_r), 2 (n \cdot \omega_h) (n \cdot \omega_i)\}$$

 $(\omega_r \cdot \omega_h) (\omega_r \cdot \omega_h)$

V-shaped grooves

Fresnel Reflectance

- Reflection from a surface is view dependent
- Fresnel equations
 - Maxwell's equations at smooth surfaces nt
 - index of refraction and polarization!
- Two kinds of Fresnel equations:
 - Dielectric materials (insulators) reflection & transmission
 - Conductors (metals) only reflection & some absorption



ηi

Dielectric Fresnel

• Fresnel reflectance for parallel polarized light r₁:

 $\mathsf{R}_{\scriptscriptstyle \parallel} = \left| \frac{\mathsf{\eta}_{\mathsf{t}} \cos \theta_i - \mathsf{\eta}_{\mathsf{i}} \cos \theta_t}{\mathsf{\eta}_{\mathsf{t}} \cos \theta_i + \mathsf{\eta}_{\mathsf{i}} \cos \theta_t} \right|^2$



• Fresnel reflectance for perpendicular polarized light r.:

$$\mathsf{R}_{\perp} = \left| \frac{\eta_{\mathrm{i}} \cos \theta_{\mathrm{i}} - \eta_{\mathrm{t}} \cos \theta_{\mathrm{t}}}{\eta_{\mathrm{i}} \cos \theta_{\mathrm{i}} + \eta_{\mathrm{t}} \cos \theta_{\mathrm{t}}} \right|^{2}$$

- Unpolarized reflectance $F_r = \frac{1}{2}(R_{\parallel} + R_{\perp})$.
 - Transmittance $T_r = 1 F_r$.



- R_p parallel polarized, R_s perpendicular polarized
- Schlick approximation given reflectance R₀

Conductors Fresnel

And

• No transmission, but some absorption k:

 $R_{II} = \frac{(\eta^2 + k^2) \cos\theta_i^2 - 2\eta \cos\theta_i + 1}{(\eta^2 + k^2) \cos\theta_i^2 + 2\eta \cos\theta_i + 1}$

 $\mathsf{R}_{\scriptscriptstyle \perp} = \frac{(\eta^2 + k^2) - 2\eta \cos\theta_i + \cos\theta_i^2}{(\eta^2 + k^2) + 2\eta \cos\theta_i + \cos\theta_i^2}$

Conductors Fresnel



- No transmission, complex index of refraction: η, k
- High reflectance across angles of incidence

BRDF Measurement

- Analytical models have limitations
 - describe specific kinds of surfaces
 - appropriate parameters not easy to obtain!
- Measurement of BRDFs a solution
 - direct usage as tabulated data
 - fit to analytic models or basis functions

Dense Measurements



- Gonioreflectometer
 - Cornell, CUReT, NIST
 - Missing measurements interpolation!

Goneo-reflectometer



DMS 803 6 motorised axis



SOC210-BDR

LED-based Measurement



[Ben-Ezra et al. 08]

- LEDs as emitters as well as sensors!
- Parallel measurements with point sampling

Image-based Measurements



[Marschner et al. 00]



[Matusik et al. 03]



100 BRDFs MERL database

Spherical Sample (Isotropic BRDF = 3D function)





More than 100 different BRDFs

20-80M Reflectance Measurements per Material





Standard



Standard

Incident: $\omega_i = (\theta_i, \Phi_i)$



Standard

Incident: $\omega_i = (\theta_i, \Phi_i)$ Exitant: $\omega_o = (\theta_o, \Phi_o)$



Standard

Incident: $\omega_i = (\theta_i, \Phi_i)$ Exitant: $\omega_o = (\theta_o, \Phi_o)$

Rusinkiewicz

Halfway: $\omega_h = (\theta_h, \Phi_h)$



Standard

Incident: $\omega_i = (\theta_i, \Phi_i)$ Exitant: $\omega_o = (\theta_o, \Phi_o)$

Rusinkiewicz

Halfway: $\omega_h = (\theta_h, \Phi_h)$ Difference: $\omega_d = (\theta_d, \Phi_d)$

Advantage:

Specular highlight Around halfway vector



Rusinkiewicz

Halfway: $\omega_h = (\theta_h, \Phi_h)$ Difference: $\omega_d = (\theta_d, \Phi_d)$



Standard

Reparameterization ω_i





Full Rank!




Low Rank!

Reparameterization ω_{d} 1.5 1 0.5 0 1.5 ω_h 1 0.5 0 -0.5 1.5 -1 0.5 0 -0.5 -1.5 -1 -1.5 Sample Densely Rusinkiewicz

Reparameterized data

Tabulated: 90 (θ_h) x 90 (θ_d) x 360 (ϕ_d)

• Easy to use in rendering system

Disadvantages:

- Requires 17Mb / BRDF
- 12 Hours to capture

Direct Visualization (Tabulated)



Data-driven BRDF Representations

Data-driven Analysis

- Linear Data Analysis (PCA)
- Non-linear Data Analysis
- BRDFs as data driven basis

[Matusik et al. 2003]

Linear Data Analysis (PCA)

- Linearize each BRDF in a (long) vector
- Apply PCA on all these vectors
- Keep n largest principal vectors



Linear Data Analysis (PCA)

- Linearize each BRDF in a (long) vector
- Apply PCA on all these vectors
- Keep n largest principal vectors



PCA space exploration



Problem: non-physical BRDFs

45D space contains non-physical BRDFs



Measured BRDF

(point A in 45D space)

Non-physical BRDF

(point close to A in 45D space)









Move a little => fall outside measured space







Only move over manifold!

Non-linear Data Analysis





Local Linear Embedding

Non-linear Data Analysis



Non-linear Data Analysis

Charter Method [Brand 2003]: kernel-based mixtures of projections that minimizes distortions of local neighborhoods



Non-linear manifold exploration



BRDFs as Basis Functions

Representing a new BRDF as a linear combination of the 100 measured BRDFs



Solution

Linear equation: b = Pa

```
b = linearized BRDF (4M \times 1) (new data)
```

P = matrix of all BRDFs (4M x 100) (MERL database)

a = unknowns (100 x 1)

Hugely over-constrained (many more knowns than unknowns)

Alternate randomized solution

• 800 rows from the original P (randomly selected)

b' = P'a

- b' = 800 x 1 vector
- P' = 800 x 100 vector
- $a = 100 \times 1 \text{ vector}$

• 800 (ω_i , ω_o) samples (measurements)

BRDFs as Basis Functions



BRDFs based on 800 samples

Optimal BRDF sampling

[Neilson et al. 15]



- Up to 5 views sufficient for spherical samples
- Fitting based on projection to space spanned by 100 MERL BRDFs

Optimal BRDF sampling

[Neilson et al. 15]



Material	n=1 $n=2$		n=5	Refe	Reference	
black-soft-plastic						
blue-acrylic					-	
blue-metallic-paint2						
green-fabric						
cayman [Cornell]						
garnet-red [Cornell]						
krylon-blue [Cornell]						

Image-based Measurements



Catadioptric Measurements









[Kuthirummal&Nayar 06]

Mirrors

Catadioptric Measurements





Catadioptric Measurements



- Mukaigawa et al. point sample the BRDF
- Ghosh et al. project basis functions



[Mukaigawa et al. 07]

Basis Illumination







$$\hat{f}_r(\boldsymbol{\omega}_i, \boldsymbol{\omega}_o) = f_r(\boldsymbol{\omega}_i, \boldsymbol{\omega}_o) \cos \theta_i \approx \sum_k Z_k(\boldsymbol{\omega}_i) z_k(\boldsymbol{\omega}_o),$$

$$z_k(\omega_o) = \int_{\mathbf{Z}} Z_k(\omega_i) f_r(\omega_i, \omega_o) \cos \theta_i \, d\omega_i.$$

- Zonal basis functions (related to spherical harmonics)
- Coefficients of BRDF in the basis recorded

Basis Illumination





- Zonal basis functions (related to spherical harmonics)
- Coefficients of BRDF in the basis recorded

SVBRDF (Spatially Varying BRDFs)



SVBRDF

- •6D function (Surface position, incident, exitant)
- •Planar surfaces
- Many independent surface points with different BRDFs
- •Not a simple texture!



Question

- •How to efficiently capture and model?
 - Analytic
 - Data-driven
 - Statistical/Frequency domain modeling

Linear Light Source Reflectometry

Andrew Gardner, Chris Tchou, Tim Hawkins, and Paul Debevec, SIGGRAPH 2003

Linear Light Source Reflectometry

EOS-1 Ds

DIGITAL

SVBRDF sample

Linear light source

Legos
SVBRDF Parameters



Diffuse Intensity

Specular Intensity

Specular Roughness



Translucency

Normals (X & Y gradients)

Displacement

Motivation: Linear Light Source



- Fewer images needed to cover planar samples with linear light source
- Dynamic range compression compared to point light source
 - can be photographed with single exposure instead of HDR
- Simple machinery of linear 1D translation to cover entire sample

Capture



Reflectance trace for each pixel

X-axis: time (light motion)

Y-axis: reflectance

Diffuse peak td coincides with light aligned with surface normal

Specular peak tm coincides with light aligned with mirror reflection



- 1. Fit diffuse
- 2. Subtract diffuse
- **3.** Estimate mean and variance of specular
- 4. Look-up specular parameters



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- 1. Fit diffuse
- 2. Subtract diffuse
- 3. Estimate mean and variance of specular



Results



Pocket Reflectometry





Ren et al. SIGGRAPH 2011

Pocket Reflectometry



BRDF chart



plaster	sliver paint	rubber	polished acrylic	aluminium	fluorescent paint
matte tape	black paper	polished resin	bronze	bronze metallic paint	acrylic
plastic	brass	coated metallic paint	polyethylene	red metallic paint	alumina
80% Spectralon	leather	matte golden paint	alum-bronze	tinfoil	lactoprene

Pocket Reflectometry



Time-shift compensation



- Different surface points will have their peaks at different time (frame)
- Reflectance trace of BRDF chart cannot be directly compared with sample

Dynamic time warping



Frame #

Frame #

Frame #

Frame #

Frame #

900

900

900

900

900

800

800

800

800

800

Alignment of reflectance traces of BRDF chart with sample

Reflectance estimation from chart

$$\mathbf{r} = d \, \mathbf{a} + s \, \mathbf{b},$$

$$a(t) = \int_{\Omega^+} L_t(\mathbf{i}) \,\alpha(\mathbf{i}, \mathbf{o}) \,(\mathbf{n} \cdot \mathbf{i}) \,\mathrm{d}\mathbf{i}, \quad b(t) = \int_{\Omega^+} L_t(\mathbf{i}) \,\beta(\mathbf{i}, \mathbf{o}) \,(\mathbf{n} \cdot \mathbf{i}) \,\mathrm{d}\mathbf{i},$$

$$\min_{u_0,u_1,\cdots,u_k} \left\| \mathbf{r} - u_0 \, \mathbf{a} - \sum_{j=1}^k u_j \, \mathbf{b}_j \right\|, \quad u_j \ge 0, \ \mathbf{b}_j \in \Phi(\mathbf{r})$$

- a diffuse BRDF with albedo d
- b specular BRDF with parameters s
- Instead of direction estimation of s, estimate a linear combination of k exemplar BRDFs in BRDF chart

Bumpy surface estimation



- Compute surface normal as intersection of two orthogonal passes of light source to estimate X & Y components of surface normals
- Assumption mostly flat surface, so no need to estimate z component

Bumpy surface results



Flat surface results



Real Photo in Incandescent Bulb

Rendering Result in Incandescent Bulb

Rendering Results in Natural Environmental Lighting

Measure and fit

- Analytic BRDF models
 - albedo
 - specular roughness
 - normal and tangent directions



• Is **DIRECT** estimate possible?

2nd order statistics of reflectance [Ghosh et al. 09]

- Specular reflection
 - measure of variance σ² about
 mean μ
 - reflection vector and specular roughness
 - computational illumination for optical measurement of reflectance statistics!





0th, 1st & 2nd moments

- In 1D, the moments of f(x):
 - total energy a
 - mean µ
 - variance σ^2

$$\alpha = \int \mathbf{f}(x) \, dx = L_0,$$

$$\mu = \int x \frac{\mathbf{f}(x)}{\alpha} \, dx,$$

$$= \frac{1}{\alpha} \int x \, \mathbf{f}(x) \, dx = \frac{L_1}{L_0},$$

$$\sigma^2 = \int (x - \mu)^2 \frac{\mathbf{f}(x)}{\alpha} \, dx,$$

$$= \frac{L_2}{L_0} - \frac{L_1^2}{L_0^2}.$$

Oth spherical moment



1st spherical moment



2nd spherical moment



Need to compute statistics in local shading frame!

Isotropic material

• Anisotropic material





normal tangent bitangent

Spherical harmonics



- Steerable spherical basis
 - SH basis can be rotated over the 3D sphere
- Capture reflectance with fixed SH patterns
 - Computation steering in post-process for rotations





normal tangent bitangent

Spherical harmonics



- Anisotropic material
 - σ_x^2 and σ_y^2

Isotropic reflectance



spec. normal

spec. albedo

spec. roughness

rendering

photograph

Anisotropic reflectance





spec. normal

spec. albedo

anisotropy

 (σ_x / σ_y)

tangent

bitangent

rendering

photograph

Flat sample





- Project 2nd order gradients from LCD screen
 - Sufficient to cover specular lobe of flat samples
- Screen is already polarized
 - Diffuse specular separation

Flat sample

- Project 2nd order gradients from LCD screen
 - Sufficient to cover specular lobe of flat samples
- Screen is already polarized
 - Diffuse specular separation





Specular materials!



Specular materials!





LED sphere

Continuous spherical harmonic illumination

[Tunwattanpong et al. 2013]






Hardware setup



continuous illumination

SH illumination



Diffuse-specular separation



Specular response only!



Diffuse-specular separation



Oth order energy



1st order energy



2nd order energy



3rd order energy!



5th order energy!



Constant illumination



Diffuse albedo



Reflectometry from SH



Harmonics







Specular roughness



Stereo reconstruction



diffuse albedo

specular albedo

reflection vector



5 cameras = 5 views

Stereo reconstruction



diffuse albedo

specular albedo

reflection vector



5 cameras × 5 rotations = 25 views

Stereo reconstruction



photograph

reconstructed geometry

Rendering with geometry & reflectance



Validation



photograph

Fourier basis measurement [Aitalla et al. 2013]





- Fourier basis illumination
 - Spectrum decay measure of glossiness

Fourier basis measurement [Aitalla et al. 2013]



- Fourier basis illumination
 - Spectrum decay measure of glossiness
 - Surface normal inferred from position (phase of Fourier basis) on screen

Fourier basis measurement [Aitalla et al. 2013]









0

0

 $egin{aligned} S_0 &= I \ S_1 &= Ip\cos 2\psi\cos 2\chi \ S_2 &= Ip\sin 2\psi\cos 2\chi \ S_3 &= Ip\sin 2\chi \end{aligned}$



Poincare sphere

Right-hand circularly polarized

- Stokes reflectance field
 - Mueller calculus

$$\mathbf{s}' = \mathbf{C}(\phi)\mathbf{D}(\delta;\mathbf{n})\mathbf{R}(\theta;\mathbf{n})\mathbf{C}(-\phi)\mathbf{s}$$

$$\mathbf{C} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos 2\phi & -\sin 2\phi & 0 \\ 0 & \sin 2\phi & \cos 2\phi & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

$$\mathbf{R} = \begin{pmatrix} \frac{\mathbf{R}_{\parallel} + \mathbf{R}_{\perp}}{2} & \frac{\mathbf{R}_{\parallel} - \mathbf{R}_{\perp}}{2} & 0 & 0\\ \frac{\mathbf{R}_{\parallel} - \mathbf{R}_{\perp}}{2} & \frac{\mathbf{R}_{\parallel} + \mathbf{R}_{\perp}}{2} & 0 & 0\\ 0 & 0 & \sqrt{\mathbf{R}_{\parallel} \mathbf{R}_{\perp}} & 0\\ 0 & 0 & 0 & \sqrt{\mathbf{R}_{\parallel} \mathbf{R}_{\perp}} \end{pmatrix}$$



• Stokes reflectance field

$$\mathbf{s}' = \mathbf{C}(\phi)\mathbf{D}(\delta;\mathbf{n})\mathbf{R}(\theta;\mathbf{n})\mathbf{C}(-\phi)\mathbf{s}$$

- Mueller calculus







Mobile camera-flash measurements!



Stationary materials [Aittala et al. 15]



Isotropic SVBRDFs [Riviere et al. 16]

Stationary materials [Aitalla et al. 2015]



- Two shot capture!
 - Ambient + flash image
 - Repeating texture/material
 - Statistical appearance sharing



SVBRDF Decomposition



Stationary materials [Aitalla et al. 2015]



Stationary materials [Aitalla et al. 2015]

	Diffuse	Specular	Anisotropy	Glossiness	Normals	Photo	Relit master	Photo	Relit master
	albedo	albedo	Anisouopy	Clossificss	INOTIMAIS	(center)	(center illum.)	(side)	(side illum.)
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Mobile surface reflectometry

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[Riviere et al. 16]



- backscatter measurements
- rough specular BRDFs




Data registration

- Feature extraction (Harris corners)
 - Matched with optical flow
- Homography-based warping



Frame 1

Frame i

Frame N

Light/view direction estimation

- $\omega_i = \omega_r$ (back scattering direction)
- Android standard API (getRotationMatrix)



- 3D tracking
 - Simultaneous Localisation And Mapping (PTAM [G. Klein and D. Murray 2007])
 - Limited to feature rich scenes
 - SfM alternate solution

[Riviere et al. 16]

Normal map: Weighted average



Normal map



[Riviere et al. 16]









[Riviere et al. 16]

Rendering – frontal view

$$\omega_i = \omega_r \uparrow \mathbf{n}$$



shaders





Rendering

Photograph

[Riviere et al. 16]

Rendering – novel view





shaders





Rendering

Photograph

[Riviere et al. 16]

Rendering – novel view







Rendering

Photograph

Material appearance recap ...



























Thank You!























